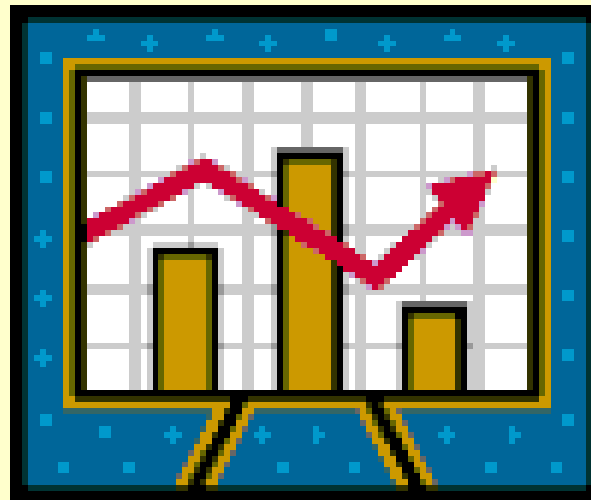


# 제 3 장

## 수요분석

### Quantitative Demand Analysis



# 彈力性

## Elasticity Concept

- Elasticity a.k.a. Sensitivity or Responsiveness
- How responsive is variable “G” to a change in variable “S”

$$E_{G,S} = \frac{\% \Delta G}{\% \Delta S}$$

If  $E_{G,S} > 0$ , then  $S$  and  $G$  are directly related.

If  $E_{G,S} < 0$ , then  $S$  and  $G$  are inversely related.

If  $E_{G,S} = 0$ , then  $S$  and  $G$  are unrelated.

## 탄력성의 계산

### Elasticity Concept Using Calculus

- An alternative way to measure the elasticity of a function  $G = f(S)$  is

$$E_{G,S} = \frac{dG}{dS} \frac{S}{G}$$

If  $E_{G,S} > 0$ , then  $S$  and  $G$  are directly related.

If  $E_{G,S} < 0$ , then  $S$  and  $G$  are inversely related.

If  $E_{G,S} = 0$ , then  $S$  and  $G$  are unrelated.

# 수요의 가격탄력성

## Own Price Elasticity of Demand

$$E_{Q_X, P_X} = \frac{\% \Delta Q_X^d}{\% \Delta P_X}$$

- Negative according to the “law of demand.”

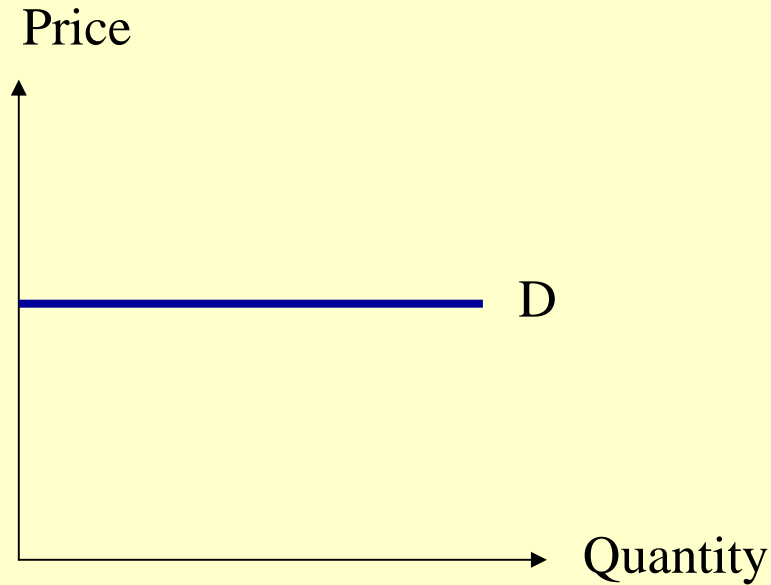
Elastic:  $|E_{Q_X, P_X}| > 1$

Inelastic:  $|E_{Q_X, P_X}| < 1$

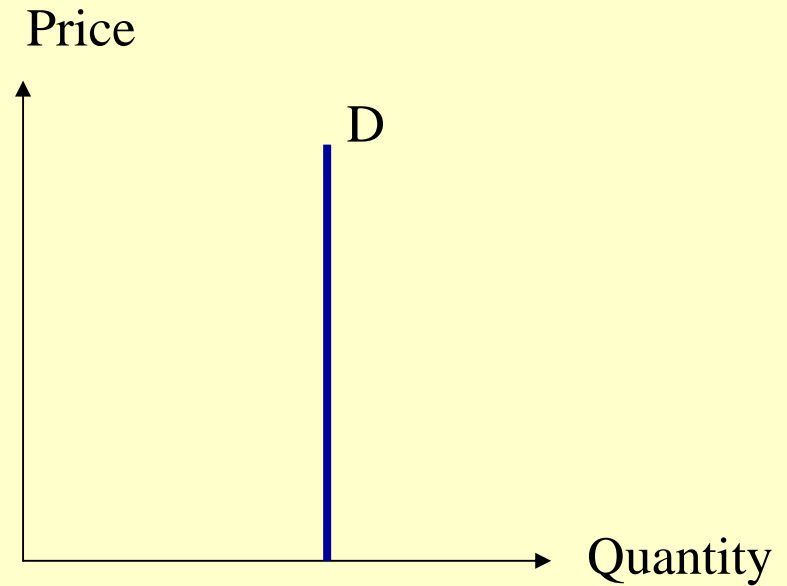
Unitary:  $|E_{Q_X, P_X}| = 1$

# 완전탄력적/비탄력적 수요

## Perfectly Elastic & Inelastic Demand



Perfectly Elastic ( $E_{Q_x, P_x} = -\infty$ )



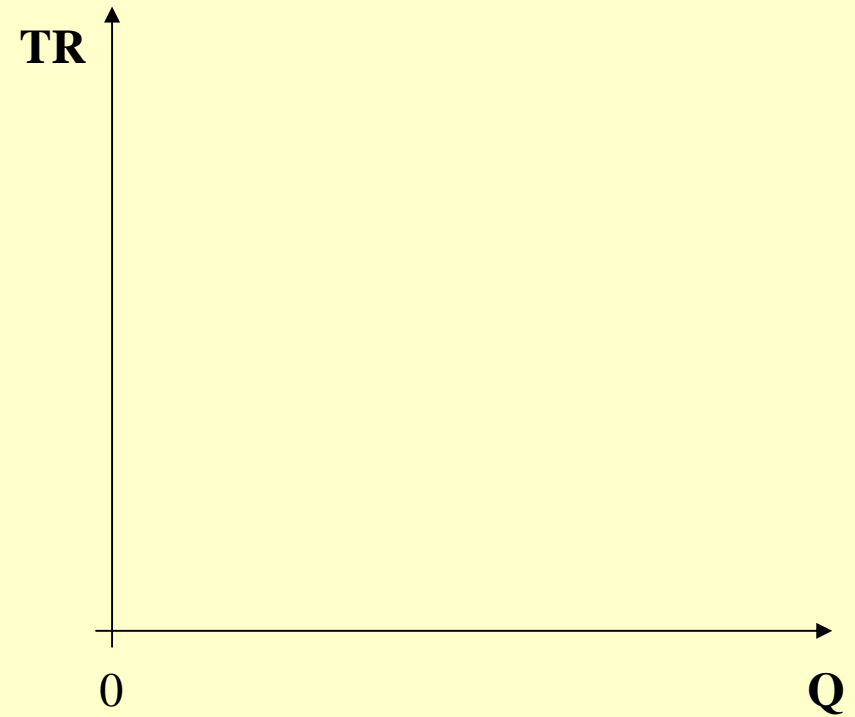
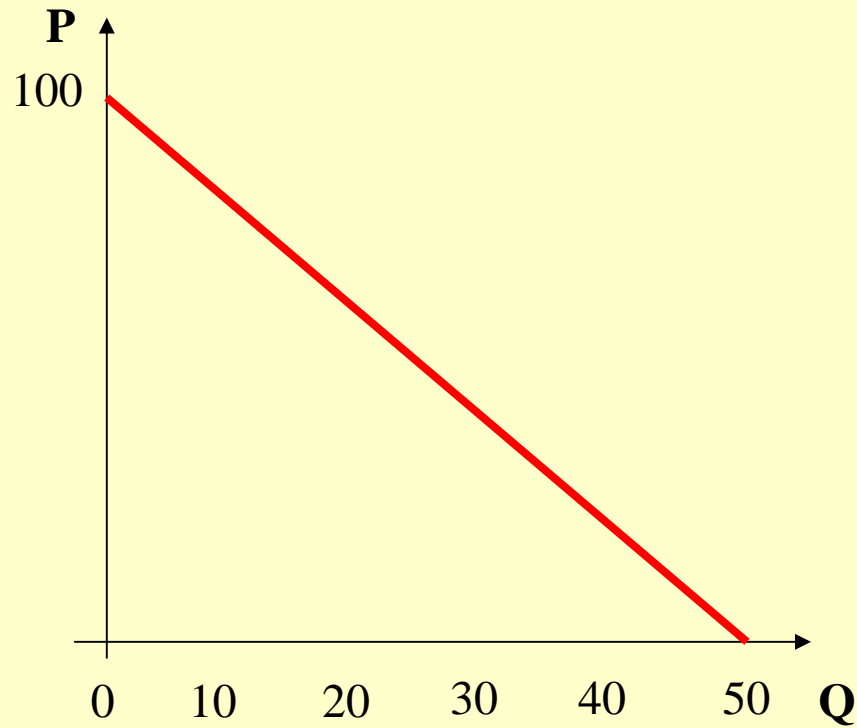
Perfectly Inelastic ( $E_{Q_x, P_x} = 0$ )

# 가격탄력성과 기업의 매출

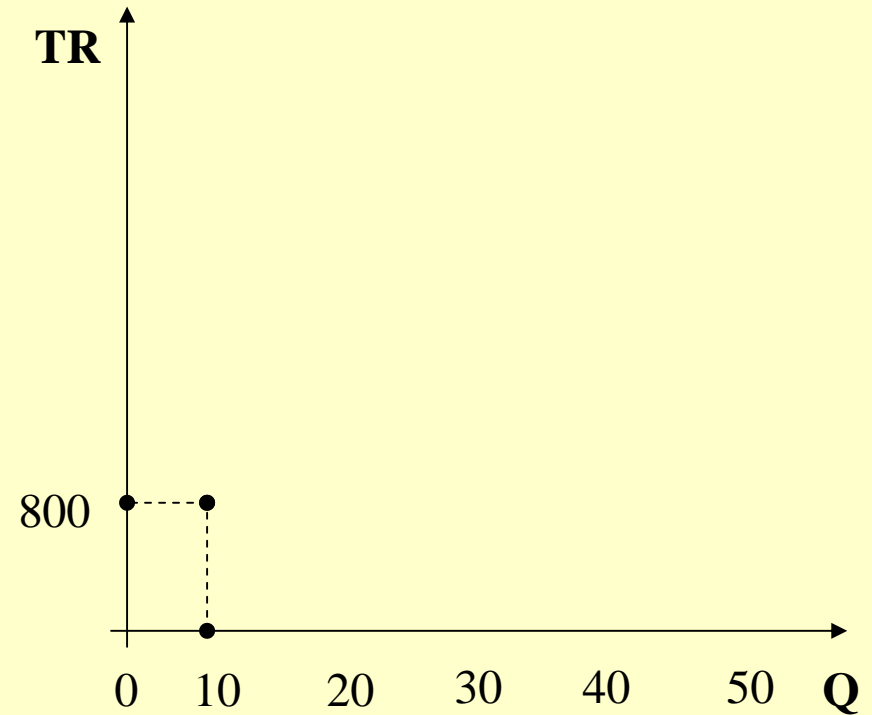
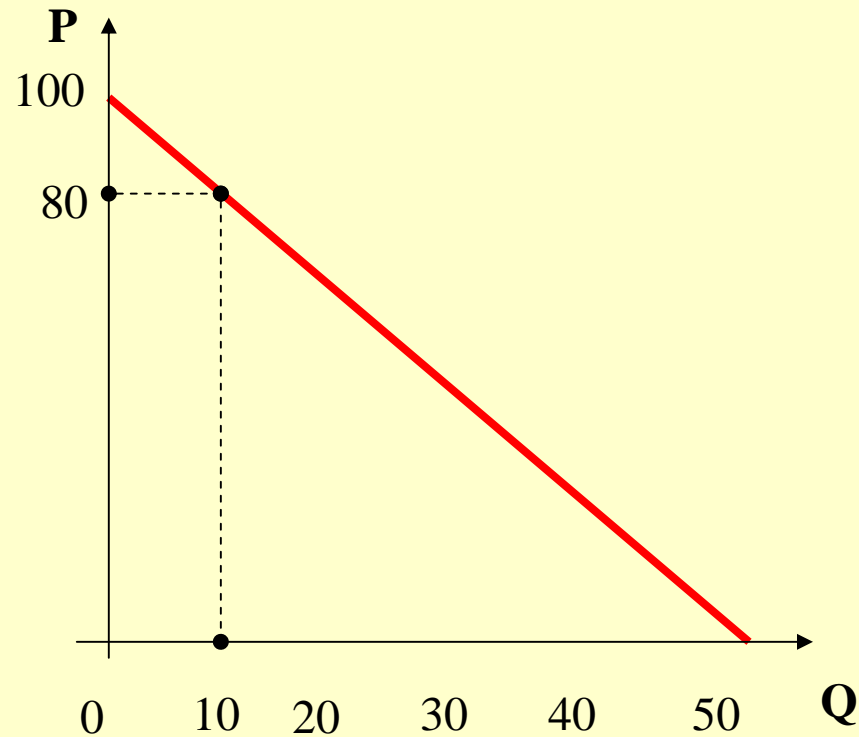
## Own-Price Elasticity and Total Revenue

- Elastic Demand
  - Increase (a decrease) in price leads to a decrease (an increase) in total revenue.
- Inelastic Demand
  - Increase (a decrease) in price leads to an increase (a decrease) in total revenue.
- Unitary Demand
  - Total revenue is maximized at the point where demand is unitary elastic.

# Elasticity, Total Revenue and Linear Demand

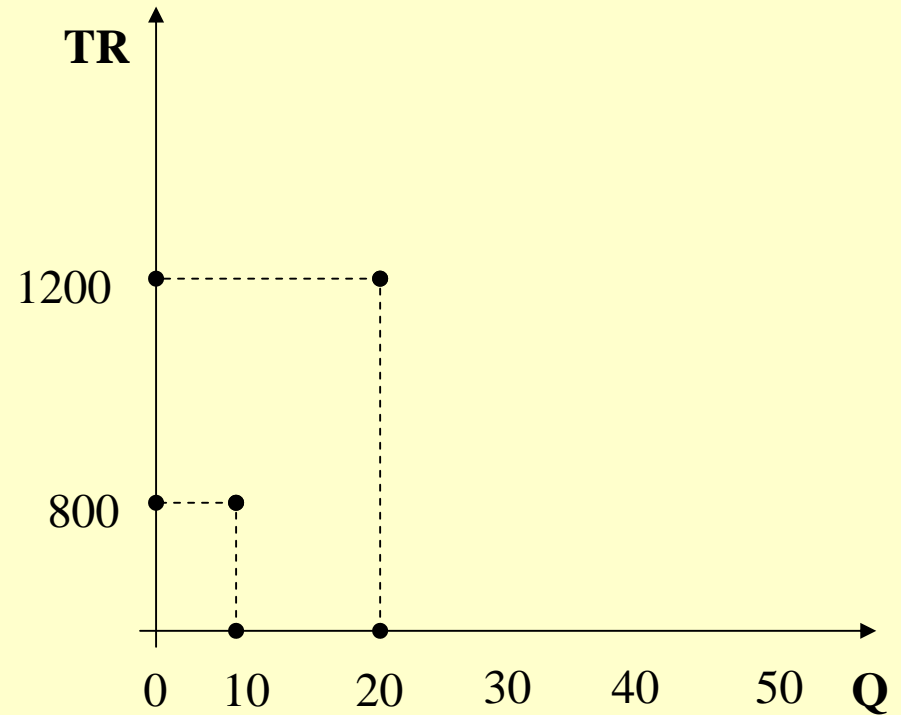
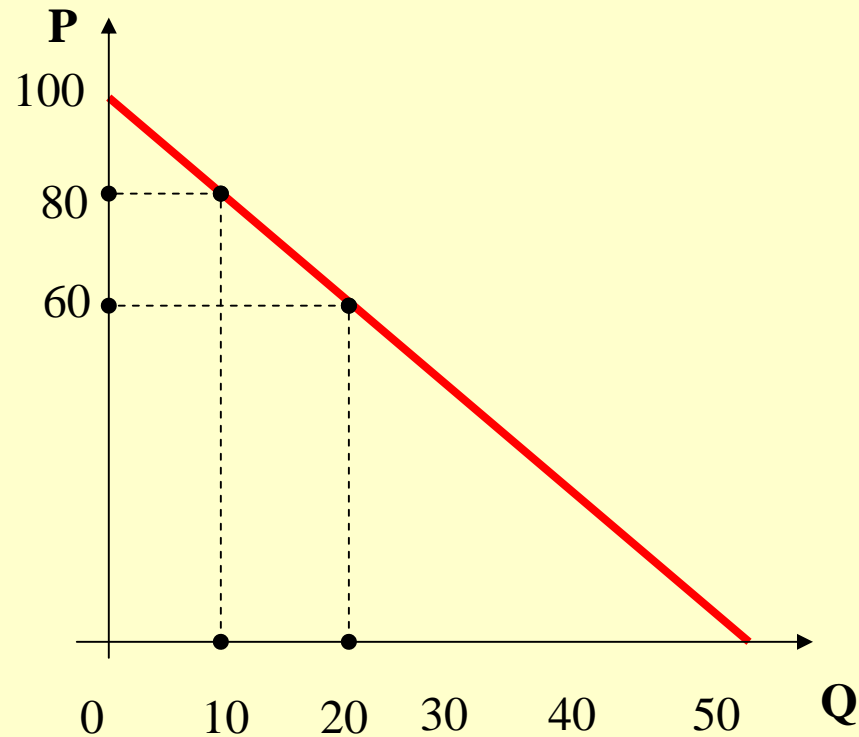


# Elasticity, Total Revenue and Linear Demand

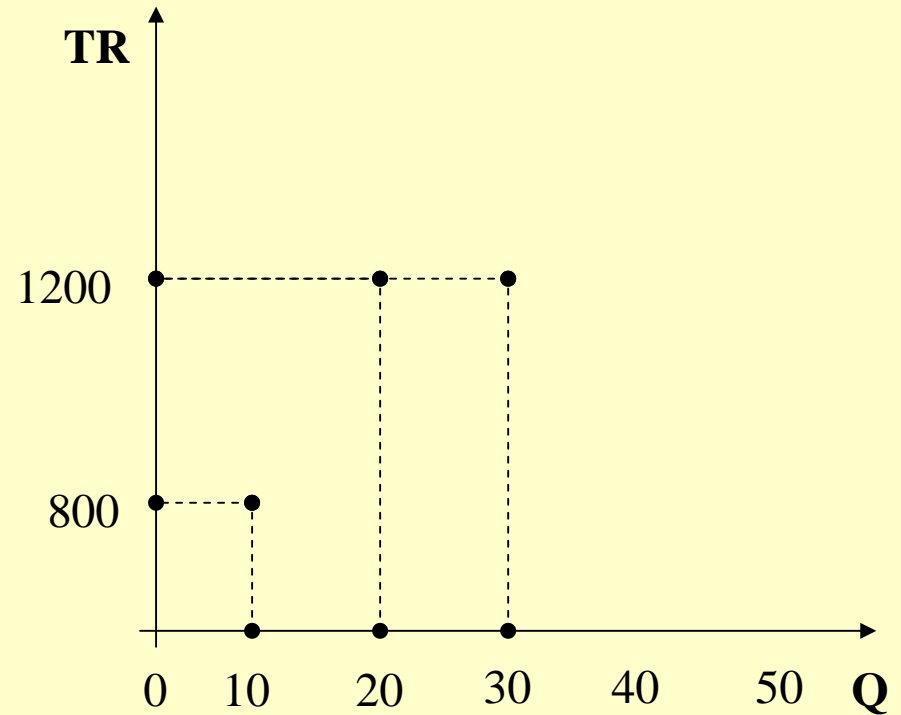
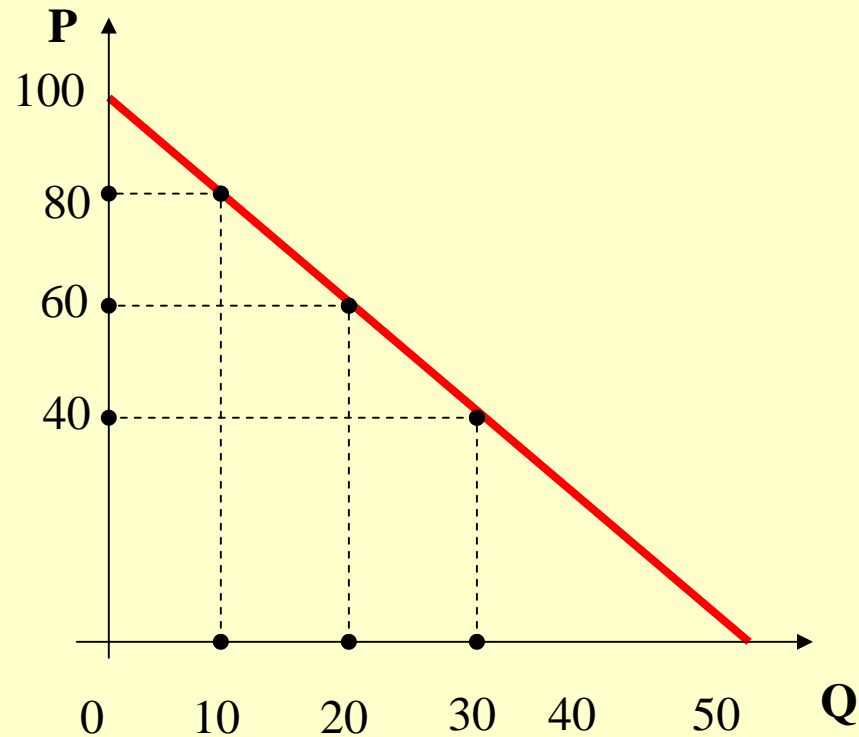




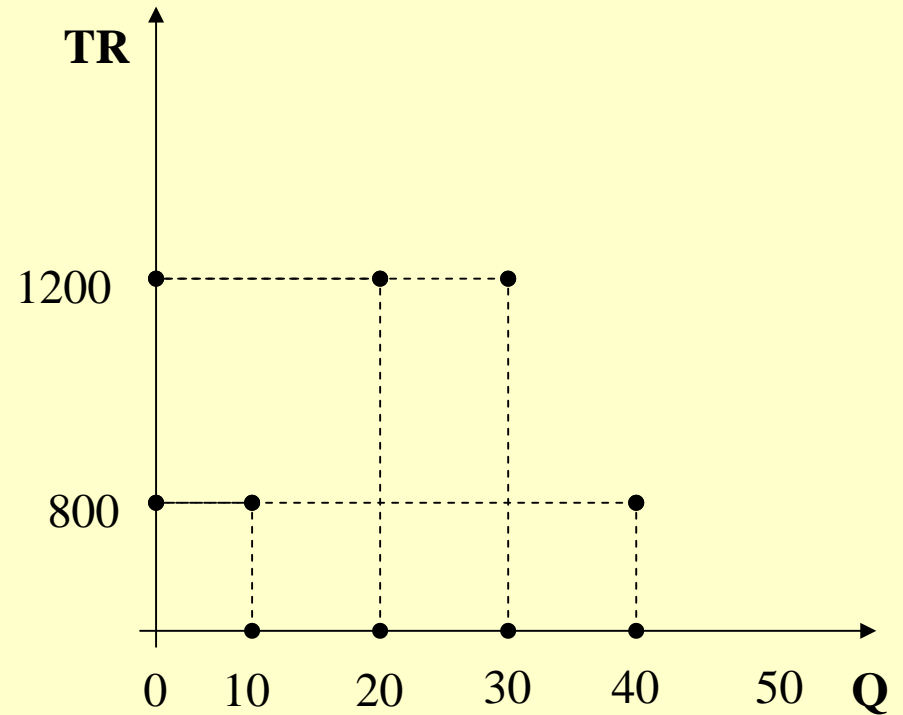
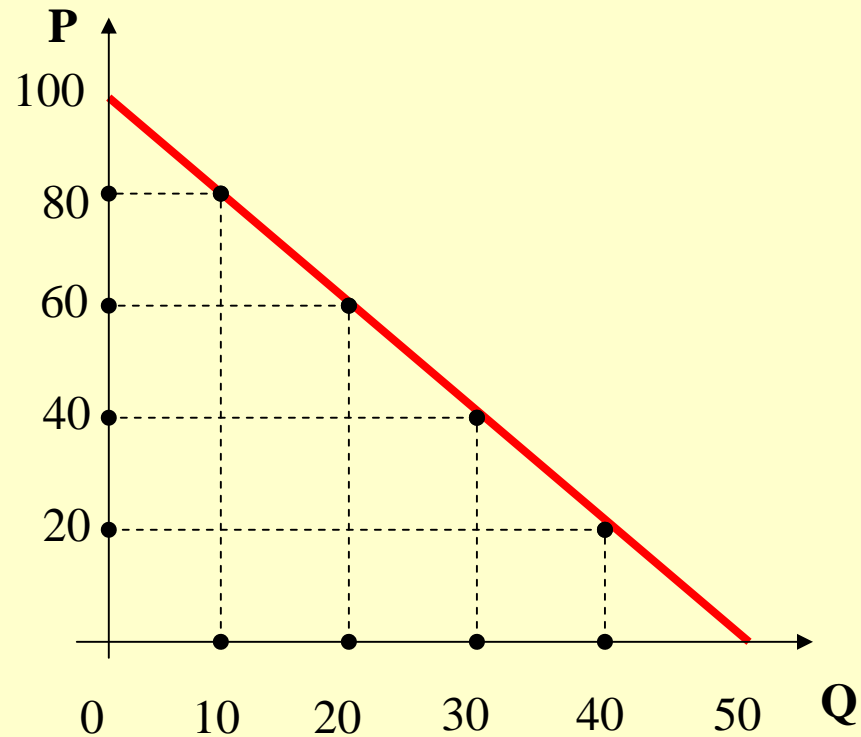
# Elasticity, Total Revenue and Linear Demand



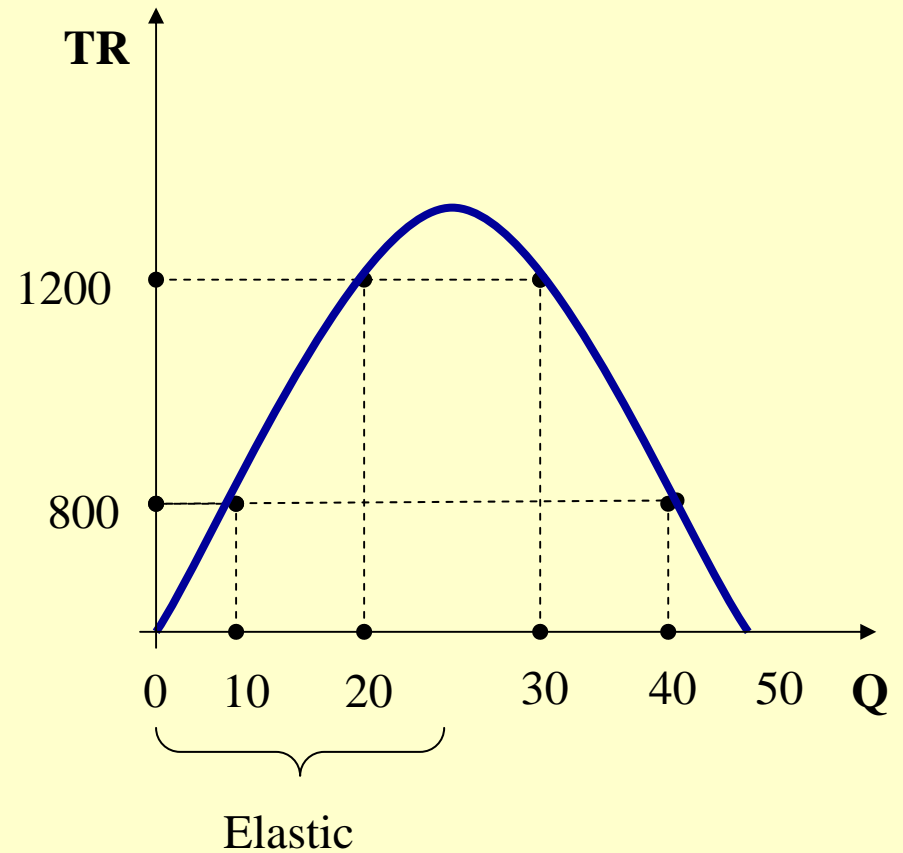
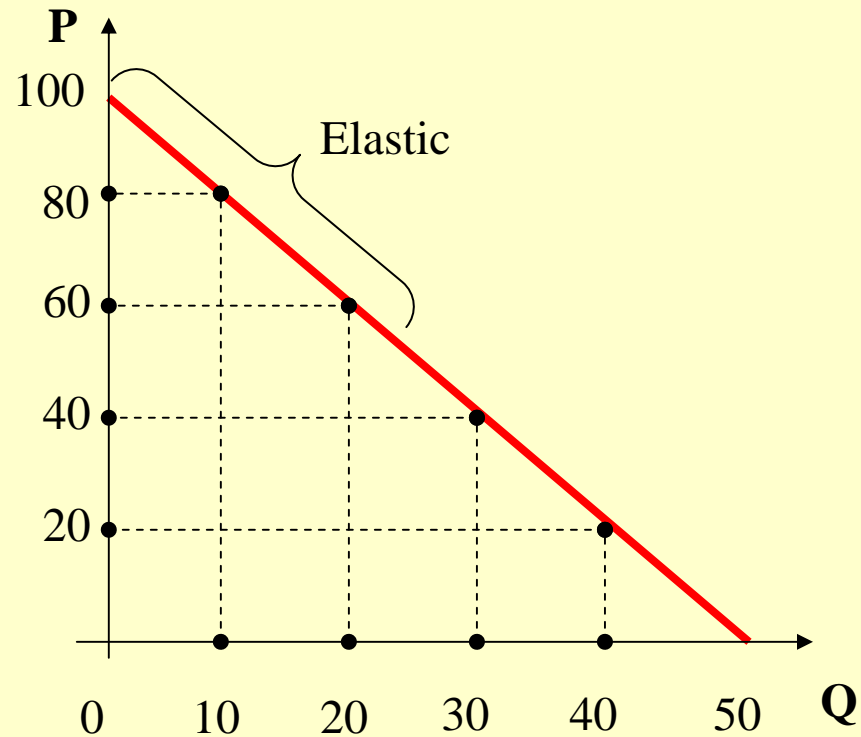
# Elasticity, Total Revenue and Linear Demand



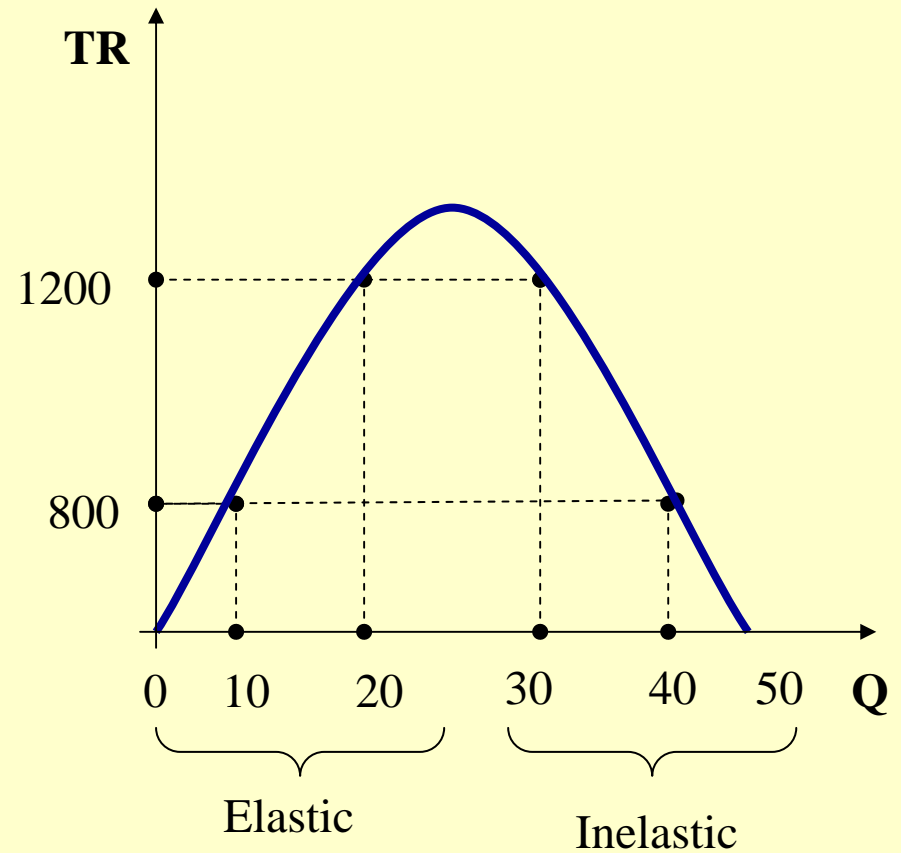
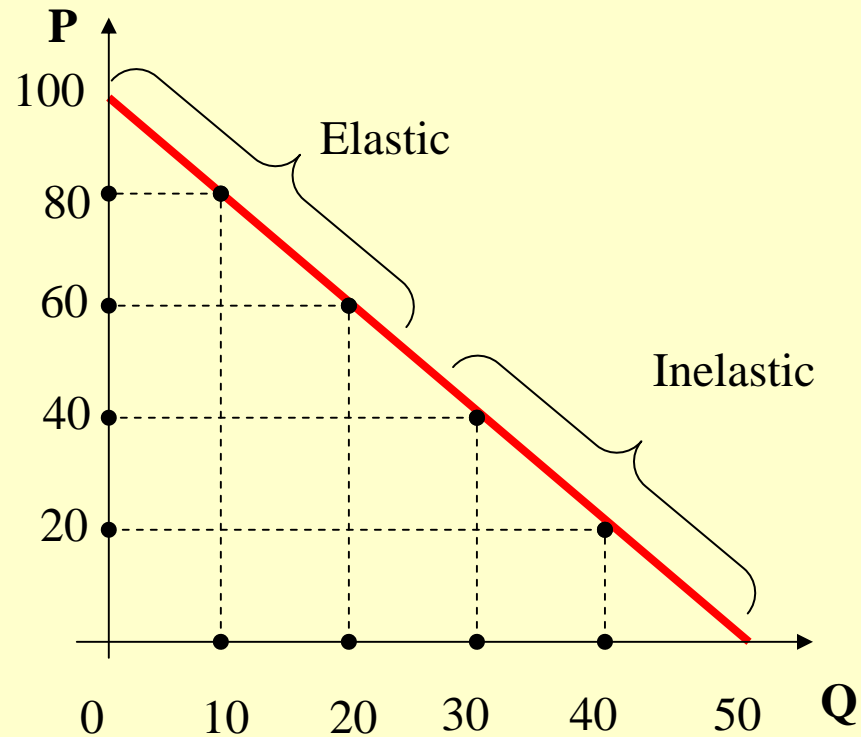
# Elasticity, Total Revenue and Linear Demand



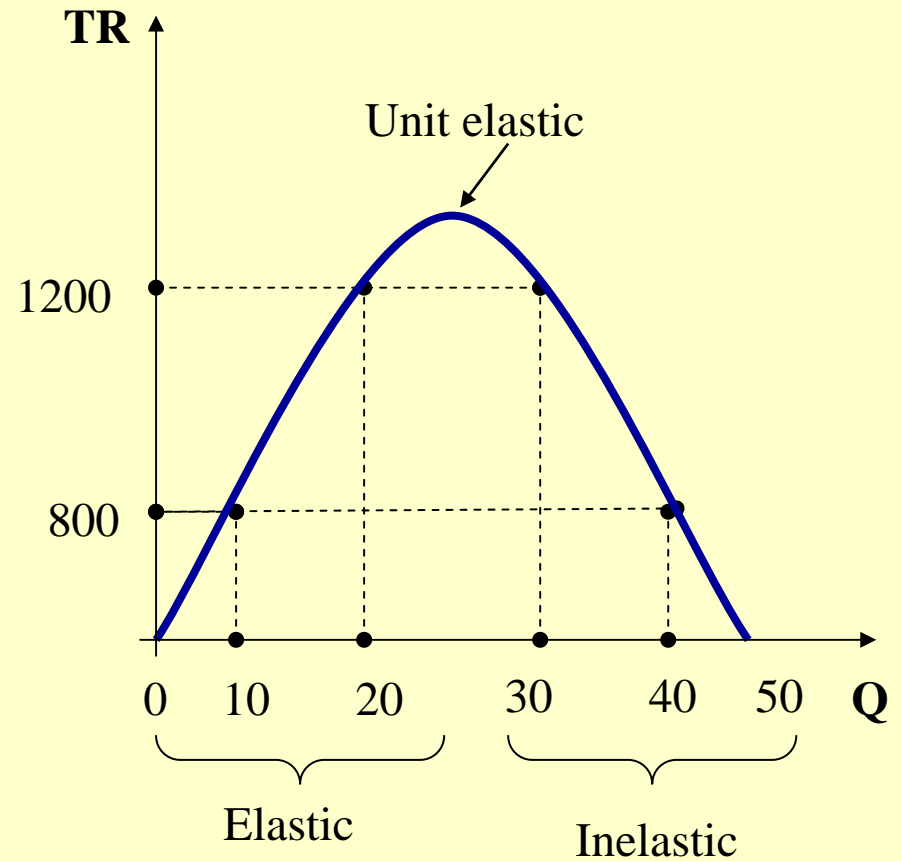
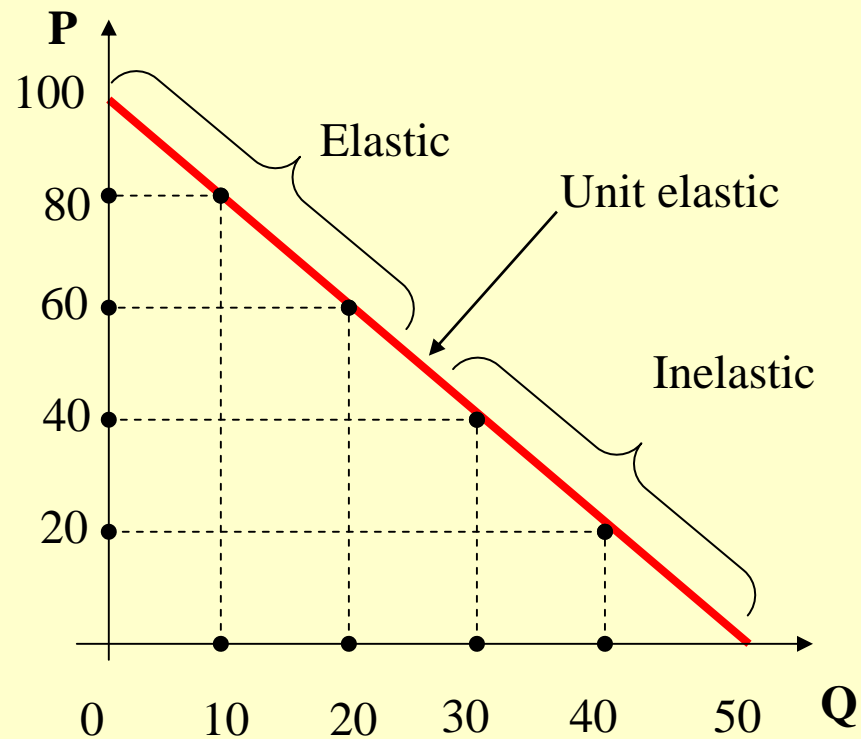
# Elasticity, Total Revenue and Linear Demand



# Elasticity, Total Revenue and Linear Demand



# Elasticity, Total Revenue and Linear Demand



# 수요의 가격탄력성에 영향을 주는 요소

## Factors Affecting Own Price Elasticity

- Available Substitutes (대체재의 유무)
  - The more substitutes available for the good, the more elastic the demand.
- Time (시간변수)
  - Demand tends to be more inelastic in the short term than in the long term.
  - Time allows consumers to seek out available substitutes.
- Expenditure Share (예산에서의 비중)
  - Goods that comprise a small share of consumer's budgets tend to be more inelastic than goods for which consumers spend a large portion of their incomes.

# 교차탄력성

## Cross Price Elasticity of Demand

$$E_{Q_X, P_Y} = \frac{\% \Delta Q_X^d}{\% \Delta P_Y}$$

If  $E_{Q_X, P_Y} > 0$ , then  $X$  and  $Y$  are substitutes (대체재).

If  $E_{Q_X, P_Y} < 0$ , then  $X$  and  $Y$  are complements (보완재).



# 소득탄력성

## Income Elasticity

$$E_{Q_X, M} = \frac{\% \Delta Q_X^d}{\% \Delta M}$$

If  $E_{Q_X, M} > 0$ , then  $X$  is a normal good (정상재).

If  $E_{Q_X, M} < 0$ , then  $X$  is a inferior good (열등재).

If  $E_{Q_X, M} = 0$ , then  $X$  is independent of income (독립재).

# 탄력성의 이용범위

## Uses of Elasticities

- Pricing.
- Managing cash flows.
- Impact of changes in competitors' prices.
- Impact of economic booms and recessions.
- Impact of advertising campaigns.
- And lots more!

# Example 1: Pricing and Cash Flows

- According to an KFTC Report, KT's own price elasticity of demand for long distance services is -8.64.
- KT needs to boost revenues in order to meet it's marketing goals.
- To accomplish this goal, should KT raise or lower it's price?

# **Answer: Lower price!**

- Since demand is elastic, a reduction in price will increase quantity demanded by a greater percentage than the price decline, resulting in more revenues for KT.

## **Example 2: Quantifying the Change**

- If KT lowered price by 3 percent, what would happen to the volume of long distance telephone calls routed through KT?

# Answer

- Calls would increase by 25.92 percent!

$$E_{Q_X, P_X} = -8.64 = \frac{\% \Delta Q_X^d}{\% \Delta P_X}$$

$$-8.64 = \frac{\% \Delta Q_X^d}{-3\%}$$

$$-3\% \times (-8.64) = \% \Delta Q_X^d$$

$$\% \Delta Q_X^d = 25.92\%$$

## **Example 3: Impact of a change in a competitor's price**

- According to an KFTC Report, KT's cross price elasticity of demand for long distance services is 9.06.
- If competitors (SKT or LGT) reduced their prices by 4 percent, what would happen to the demand for KT services?

# Answer

- KT's demand would fall by 36.24 percent!

$$E_{Q_X, P_Y} = 9.06 = \frac{\% \Delta Q_X^d}{\% \Delta P_Y}$$

$$9.06 = \frac{\% \Delta Q_X^d}{-4\%}$$

$$-4\% \times 9.06 = \% \Delta Q_X^d$$

$$\% \Delta Q_X^d = -36.24\%$$



# Interpreting Demand Functions

- Mathematical representations of demand curves.
- Example:

$$Q_X^d = 10 - 2P_X + 3P_Y - 2M$$

- X and Y are substitutes (coefficient of  $P_Y$  is positive).
- X is an inferior good (coefficient of M is negative).

# Example of Linear Demand

- $Q^d = 10 - 2P$ .
- Own-Price Elasticity:  $(-2)P/Q$ .
- If  $P=1$ ,  $Q=8$  (since  $10 - 2 = 8$ ).
- Own price elasticity at  $P=1$ ,  $Q=8$ :  
 $(-2)(1)/8 = -0.25$ .

# Log-Linear Demand

- General Log-Linear Demand Function:

$$\ln Q_X^d = \beta_0 + \beta_X \ln P_X + \beta_Y \ln P_Y + \beta_M \ln M + \beta_H \ln H$$

Own Price Elasticity :  $\beta_X$

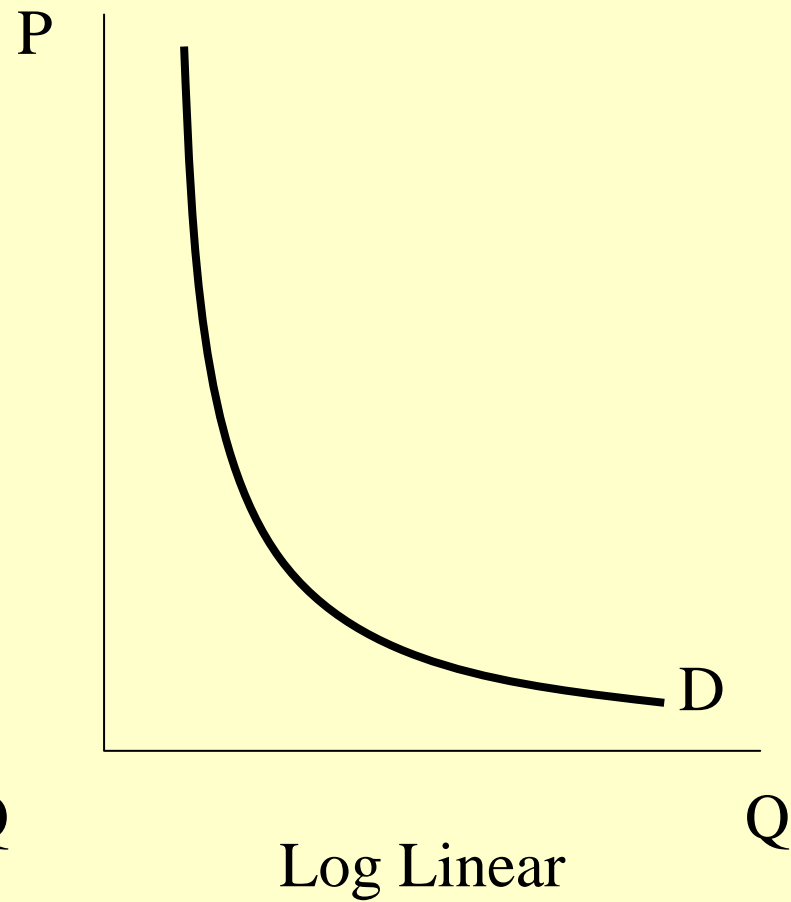
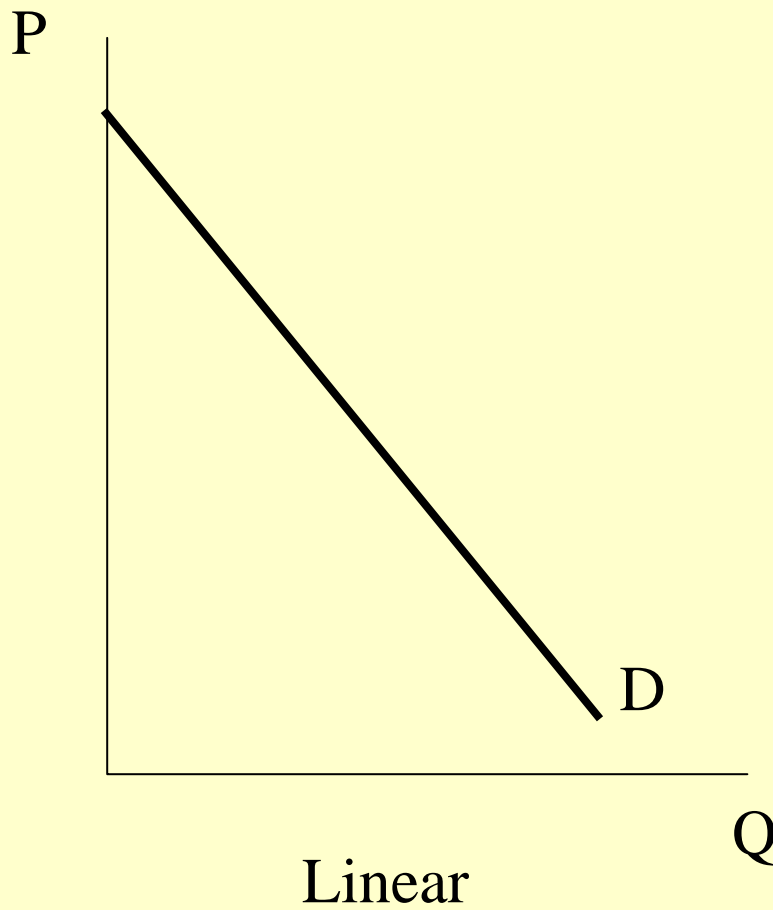
Cross Price Elasticity :  $\beta_Y$

Income Elasticity :  $\beta_M$

# Example of Log-Linear Demand

- $\ln(Q^d) = 10 - 2 \ln(P)$ .
- Own Price Elasticity: -2.

# Graphical Representation of Linear and Log-Linear Demand



# Conclusion

- Elasticities are tools you can use to *quantify* the impact of changes in prices, income, and advertising on sales and revenues.
- Given market or survey data, regression analysis can be used to estimate:
  - ◻ Demand functions.
  - ◻ Elasticities.
  - ◻ A host of other things, including cost functions.
- Managers can quantify the impact of changes in prices, income, advertising, etc.